## Influence of excited states of Mg acceptors on hole concentration in GaN

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Received 7 April 2003, revised 16 June 2003, accepted 1 August 2003 Published online 20 October 2003

PACS 61.72.Vv, 71.55.Eq, 73.61.Ey, 81.05.Ea

The influence of the excited states of the acceptors on the hole concentration in p-type GaN is investigated theoretically and experimentally. Using the temperature dependence of the hole concentration p(T) in Mg-doped GaN epilayers, a distribution function suitable for Mg acceptors is examined. It is found that the influence of their excited states on p(T) as well as the temperature dependence of the average acceptor level cannot be ignored, when the acceptor level is deep ( $\geq 150$  meV). Moreover, it is elucidated that due to their excited states the ionization efficiency of acceptors is higher at elevated temperatures than the ionization efficiency expected from the Fermi–Dirac distribution function.

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**1 Introduction** The excited states of the substitutional dopants in a semiconductor have been theoretically discussed using the hydrogenic model [1], and the existence of their excited states in Si has been experimentally confirmed using infrared absorption measurements [1]. However, the influence of their excited states on the majority-carrier concentration has not been experimentally confirmed because their excited state levels in Si are too shallow. On the other hand, an acceptor level ( $\Delta E_A$ ) in GaN or SiC, measured from the valence band maximum ( $E_V$ ), was reported to be deeper than 150 meV [2, 3]. Moreover, according to the hydrogenic model, their first excited state level ( $\Delta E_2$ ) is nearly equal to  $\Delta E_A$  of B in Si.

The Fermi-Dirac distribution function  $f_{FD}(\Delta E_A)$ , which does not consider the influence of the excited states of the acceptors, is given by

$$f_{\rm FD}\left(\Delta E_{\rm A}\right) = \frac{1}{1 + 4\exp\left(\frac{\Delta E_{\rm A} - \Delta E_{\rm F}}{kT}\right)},\tag{1}$$

where  $\Delta E_{\rm F}$  is the Fermi level measured from  $E_{\rm V}$ , k is the Boltzmann constant, and T is the absolute temperature. Using  $f_{\rm FD}(\Delta E_{\rm A})$ , the values of  $\Delta E_{\rm A}$ , the acceptor density  $(N_{\rm A})$  and the compensating density  $(N_{\rm comp})$  were determined by a least-squares fit of the charge-neutrality equation to p(T) in heavily Mg-doped GaN or Al-doped SiC. However, the obtained  $N_{\rm A}$  was much higher than the Mg or Al concentration  $(C_{\rm Mg}$  or  $C_{\rm Al})$  determined by secondary ion mass spectroscopy (SIMS) [4, 5], suggesting that this  $N_{\rm A}$  should not be reliable. Therefore, it is necessary to newly introduce a distribution function  $f(\Delta E_{\rm A})$  considering the influence of their excited states, which makes the obtained  $N_{\rm A}$  reasonable. In heavily Al-doped SiC,  $f(\Delta E_{\rm A})$  has been reported to be appropriate for the Al acceptors [6, 7].

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**2 Distribution function including excited states of acceptors** The distribution function including the influence of the excited states of the acceptors is given by [6]

$$f(\Delta E_{\rm A}) = \frac{1}{1 + 4 \exp\left(-\frac{\overline{E_{\rm ex}}}{kT}\right) \cdot \left[\exp\left(\frac{\Delta E_{\rm A} - \Delta E_{\rm F}}{kT}\right) + \sum_{r=2} g_r \exp\left(\frac{\Delta E_r - \Delta E_{\rm F}}{kT}\right)\right]},$$
(2)

where  $\Delta E_r$  is the difference in energy between the (r-1)th excited state level and  $E_v$ , and  $g_r$  is the (r-1)th excited state degeneracy factor. An ensemble average  $E_{ex}$  of their ground and excited state levels is given by [6, 7, 11]

$$\overline{E_{\text{ex}}} = \frac{\sum_{r=2} \left(\Delta E_{\text{A}} - \Delta E_{r}\right) g_{r} \exp\left(-\frac{\Delta E_{\text{A}} - \Delta E_{r}}{kT}\right)}{1 + \sum_{r=2} g_{r} \exp\left(-\frac{\Delta E_{\text{A}} - \Delta E_{r}}{kT}\right)},$$
(3)

and then an average energy level  $\overline{\Delta E_A}$  of the acceptors, measured from  $E_v$ , is expressed as [6, 7]

$$\overline{\Delta E_{\rm A}} = \Delta E_{\rm A} - \overline{E_{\rm ex}} \,. \tag{4}$$

When their excited states are neglected (i.e., r = 1 and  $\overline{E_{ex}} = 0$ ), Eq. (2) coincides with  $f_{FD}(\Delta E_A)$ .

**3 Free carrier concentration spectroscopy**<sup>1</sup> Using an experimental p(T), the FCCS signal is defined by [6–10]

$$H(T, E_{\rm ref}) \equiv \frac{p(T)^2}{(kT)^{5/2}} \exp\left(\frac{E_{\rm ref}}{kT}\right)$$
(5)

and has a peak at the temperature corresponding to each acceptor level, where  $E_{ref}$  is the parameter which can shift its peak temperature within the measurement temperature range.

From the charge-neutrality condition, in p-type semiconductors, p(T) is described as

$$p(T) = \sum_{i} N_{Ai} F(\Delta E_{Ai}) - N_{\text{comp}}, \qquad (6)$$

where  $N_{Ai}$  and  $\Delta E_{Ai}$  are the density and energy level of the *i* th acceptor species, and  $F(\Delta E_{Ai})$  represents  $f(\Delta E_{Ai})$  or  $f_{FD}(\Delta E_{Ai})$ . On the other hand, using the effective density of states  $N_V(T)$  in the valence band, p(T) is expressed as

$$p(T) = N_{\rm v}(T) \exp\left(-\frac{\Delta E_{\rm F}}{kT}\right),\tag{7}$$

where

$$N_{\rm V}(T) = N_{\rm V0} k^{3/2} T^{3/2}$$
 and  $N_{\rm V0} = 2 \left(\frac{2\pi m^*}{h^2}\right)^{3/2}$ ,

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<sup>&</sup>lt;sup>1</sup> The Windows application software for FCCS can be downloaded at our web site (http://www.osakac.ac.jp/labs/matsuura/).

 $m^*$  is the hole effective mass, and h is the Planck's constant. Substituting Eq. (6) for one of the two p(T) in Eq. (5) and substituting Eq. (7) for the other p(T) in Eq. (5) yield

$$H(T, E_{\rm ref}) = \sum_{i} \frac{N_{\rm Ai}}{kT} \exp\left(-\frac{\Delta E_{\rm Ai} - E_{\rm ref}}{kT}\right) I(\Delta E_{\rm Ai}) - \frac{N_{\rm comp}N_{\rm V0}}{kT} \exp\left(\frac{E_{\rm ref} - \Delta E_{\rm F}}{kT}\right),\tag{8}$$

where

$$I\left(\Delta E_{Ai}\right) = N_{V0} \exp\left(\frac{\Delta E_{Ai} - \Delta E_{F}}{kT}\right) F\left(\Delta E_{Ai}\right).$$
<sup>(9)</sup>

The function

$$\frac{N_{Ai}}{kT} \exp\left(-\frac{\Delta E_{Ai} - E_{ref}}{kT}\right)$$
(10)

in Eq. (8) has a peak value of  $N_{Ai} \exp(-1)/kT_{peaki}$  at the peak temperature

$$T_{\text{peak}i} = \frac{\Delta E_{\text{A}i} - E_{\text{ref}}}{k} \,. \tag{11}$$

As is clear from Eq. (11),  $E_{\text{ref}}$  can shift  $T_{\text{peak}i}$ . Although the actual  $T_{\text{peak}i}$  is slightly different from  $T_{\text{peak}i}$  calculated by Eq. (11) due to the temperature dependence of  $I(\Delta E_{Ai})$ , we can determine  $N_{Ai}$  and  $\Delta E_{Ai}$  from the peak of the experimental FCCS signal easily and accurately, using a personal computer.

**4 Experimental** 2 µm-thick Mg-doped p-type GaN epilayers were grown at 1025 °C by metalorganic chemical vapor deposition on undoped GaN/sapphire, and annealed at 800 °C in N<sub>2</sub> for 20 min. The  $C_{Mg}$  in the epilayers was  $2 \times 10^{19}$  cm<sup>-3</sup>. The p(T) was obtained by Hall-effect measurements in a magnetic field of 1.4 T.

**5 Results and discussion** The open circles and open triangles in Fig. 1 represent the experimental p(T) and  $\Delta E_{\rm F}$ . The FCCS signal (solid line in Fig. 2) is calculated by interpolating p(T) with a cubic smoothing natural spline function at intervals of 0.1 K. Since there is only one peak, this epilayer includes only one species of acceptor. From the peak, the values of  $N_{\rm A}$ ,  $\Delta E_{\rm A}$  and  $N_{\rm comp}$  are determined to be  $8.9 \times 10^{18}$  cm<sup>-3</sup>, 149 meV and  $1.5 \times 10^{17}$  cm<sup>-3</sup> for  $f(\Delta E_{\rm A})$ , and  $2.1 \times 10^{20}$  cm<sup>-3</sup>, 154 meV and  $2.2 \times 10^{18}$  cm<sup>-3</sup> for  $f_{\rm FD}(\Delta E_{\rm A})$ . Because  $N_{\rm A}$  is the concentration of Mg atoms located at the substitutional sites in GaN,  $N_{\rm A}$  should be less than or equal to  $C_{\rm Mg}$ , indicating that  $f(\Delta E_{\rm A})$  is appropriate in this Mg-doped GaN epilayer. Therefore, it is found that ~45 % of Mg atoms in this epilayer act as an acceptor.

The broken and dotted lines in Fig. 2 represent the FCCS signals simulated using  $N_A$ ,  $\Delta E_A$ , and  $N_{\text{comp}}$  for  $f(\Delta E_A)$  and  $f_{\text{FD}}(\Delta E_A)$ , respectively. Only the broken line is in agreement with the solid line, suggesting that  $f(\Delta E_A)$  is appropriate for Mg acceptors in GaN.

The open circles, and the solid and broken lines in Fig. 3 represent the experimental p(T) and two p(T) simulations using the values determined by  $f(\Delta E_A)$  and  $f_{FD}(\Delta E_A)$ , respectively. Since both the simulated p(T) coincide with the experimental p(T), it is difficult to determine which distribution function is suitable for explaining the ionization efficiency of the Mg acceptors in GaN.

Although  $N_A$  for  $f(\Delta E_A)$  is much lower than  $N_A$  for  $f_{\rm FD}(\Delta E_A)$ , the simulated p(T) using this lower  $N_A$  coincides with the experimental p(T), because according to Eq. (4) their excited states make  $\Delta E_A$  shallow at elevated temperatures. According to Poisson's equation,  $N_A$  influences the shape of the

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**Fig. 1** Experimental p(T) and  $\Delta E_{\rm F}$ .



**Fig. 2** FCCS signals with  $E_{ref} = 0.237 \text{ eV}$ .



Fig. 3 Comparison between experimental p(T) and two p(T) simulations using  $f(\Delta E_A)$  or  $f_{FD}(\Delta E_A)$  with the values determined by the corresponding distribution function. Since the p(T) simulation using  $f(\Delta E_A)$  is very close to the p(T) simulation using  $f_{FD}(\Delta E_A)$ , the solid line overlaps with the broken line.

band bending in pn junctions, indicating that in GaN devices the electric characteristics obtained by device simulation should be affected by the Mg acceptor density. Therefore, it is essential to use  $f(\Delta E_A)$  by which the accurate p(T) is obtained using the actual value of  $N_A$ .

**6 Conclusion** The distribution function considering the influence of the excited states of the acceptors was proposed. In  $f(\Delta E_A)$ , an ensemble average of their ground and excited state levels was introduced. Using  $f(\Delta E_A)$  or  $f_{FD}(\Delta E_A)$ , the experimental p(T) in p-type Mg-doped GaN was investigated. It is found that FCCS is more appropriate for investigating the influence of their excited states on p(T) than the least-squares fit of the charge-neutrality equation to p(T), and it is elucidated that  $f(\Delta E_A)$  is appropriate for acceptors in GaN. Moreover, it is essential to use  $f(\Delta E_A)$  in device simulations for GaN.

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